

# Pre Calculus

**Date:**

**Items Needed:** .Book,

**Objective:** The students will be able determine what an inverse function is and how to find it given any function.

**PA Common Core:** cc.2.2.hs.c.4

**Lesson:**

- On the overhead graph:  $f(x) = 2x - 3$  and  $f^{-1}(x) = \frac{1}{2}(x + 3)$
- To be an inverse of each other the graphs should be reflections of each other with respect to the line  $y=x$ .
- What does this mean? If the point  $(a,b)$  is on the graph of  $f$ , the point of  $(b,a)$  is on the graph of  $f^{-1}$ .
- Do example 3.
- Graph example 3 and look at the functions graphically.
- Do example 5 and verify that they are inverses of each other using the table feature of the calculator. Make sure everyone understands the coordinates with the 3 different columns in the table.
- Look at the numerical solution for example 6.
  
- What is a function?
- We have to be careful when we try to find and inverse of a function. Just because we start with a function doesn't mean that the inverse is a function.
- Have students refer to the section highlighted on p. 64 in my text. This is an example of what can't happen.
- So how can keep from doing all the work just to see if doesn't work. We can use the horizontal line test which shows that there is a one to one relationship, one x value to one y value.
- Refer to example 7 & 8
- When a function fails the horizontal test it does not have an inverse unless you restrict the domain of the function. ie the  $x^2$  function.
  
- So how do we find an inverse?
  1. Check the function with the horizontal line test.
  2. In the equation for  $f(x)$ , replace  $f(x)$  by  $y$ .
  3. Interchange the  $x$  and  $y$  variables.
  4. After you solve for  $y$ , replace  $y$  with  $f^{-1}$ .

- Quickly look over example 9, pointing out the domain.
- Do example 10. Point out that the range of the function becomes the domain of the inverse function. Make sure you watch the domain of this one.
- Look over example 11.

**Assignment:** .Have students do 2, 3, 5, 15-18, 25, 27, 28, 30, 39, 40, 50-56(even), 57, 73, 77, 92, p. 67.

**Evaluation: (Could be from any one/several of the following)**

- Responses from classroom questions
- Results of classroom sample problems
- Homework responses
- Check answer with Calculator
- End of the section exam

**Enrichment:**